DIDACTIC UNIT:
TANGENCIES AND LINKS


3rd Compulsory Secondary Education
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a.1. Draw a pair of outer tangent circumferences, which radius are $r_{1}=2.5 \mathrm{~cm}$ And $r_{2}=2 \mathrm{~cm}$.


1. Trace $O_{1}\left(r_{1}=2.5 \mathrm{~cm}\right)$; trace a radius $r_{1}$
2. Name the tangency point $T$.
3. Prolong the 2 centimetre radius to mark the second centre.
4. Go over the two circunferences.
a.2. Draw a pair of inner tangent circumferences, which radius are $r_{1}=2 \prime 5 \mathrm{~cm}$ And $r_{2}=2 \mathrm{~cm}$.

5. Trace $O_{1}\left(r_{1}=2.5 \mathrm{~cm}\right)$; trace a radius $r_{1}$
6. Name the tangency point $T$.
7. Measure the 2 centimetre radius from point $T$ on radius OT to mark the second centre.
8. Go over the two circunferences.
b. Trace two tangent straight lines ( t y $\mathrm{t}^{\prime}$ ) to the circumference $\mathrm{O}_{1}$

9. Trace $O_{1}\left(r_{1}=4 \mathrm{~cm}\right)$; trace a rad ius $r_{1}$ (anyo ne ).
10. Name the point $T$ ( tangency poin $t$ ).
11. By point $T$, trace the tangent straight line ( $\perp$ to radius $\mathrm{O}_{1} \mathrm{~T}$ ). Go over the straight line t .
12. Trace a second rad ius $r^{\prime}$ : trace the tangent straight line $t^{\prime}$ by $\mathrm{T}^{\prime} \quad \perp$ radio $\mathrm{O}_{\mathrm{T}} \mathrm{T}^{\prime}$. Go over $\mathrm{t}^{\prime}$.

## Tangency exercises $\mid$ Sheet 2

a. Draw the circunference $O_{1}$ tangent to the straight line $t$ by poin $t \mathbf{T}$ which contains the point $\mathbf{P}$.


1. Draw the straight line $t$, mark the point $T$, anyone which belongs to $t$, and the point $P$, anyone outer to line $t$.
2. Trace the straight line $\mathbf{r} \perp$ to line $\mathbf{t}$ by point $\mathbf{T}$.
3. Join points $\mathbf{T}$ and $\mathbf{P}$.
4. Trace the perpendicular bisector of segment TP ; it cuts the line $\mathbf{r}$ by the centre O1
5. Draw the solution circumference, with centre $=\mathrm{O}_{1}$ and radius $=\mathrm{O}_{1} \mathrm{~T}$
b. Draw the tangent arc to two perpendicular straight line, which rad ius is 4 centimetre.

6. Trace two straight lines; a horiaontal one H and a vertical one v .
7. Trace a parallel one to $h$ at a 4 centimetre distance.
8. Trace a parallel one to v at a 4 centimetre distance.
9. The intersection point bet ween both parallels is the centre $O$
10. Determine the tangency points.
11. Trace the circumference arc $\mathrm{TT}^{\prime}$, which centre $=\mathrm{O}_{1}$ and radius $=\mathrm{O}_{1} \mathrm{~T}$.

## Tangency exercises 1 Sheet 3

a. Place the circumference $O$ ( radius $=2^{\prime} 5 \mathrm{~cm}$ ) and the horizontal straight line h ,

Trace the circumference $O_{1}$ ( radius $=3 \mathrm{~cm}$ )


4. Trace parallel straight line to $h$ at a 3 centimetre distance.
5. Name $\quad \mathrm{O}_{1}$ (intersection point between the arc and line $\mathrm{h}^{\prime}$ )
6. Determine T and $\mathrm{T}^{\prime}$ : trace $\mathrm{O}_{1}$; go over the solution circumference.
b. Place the circumference $O$ ( radiius $r=3 \mathrm{~cm}$ ), point $P$, outer to the circumference, and point $T$, inner to the circumference, draw the circumference $\mathrm{O}_{1} \mathrm{t}$ angent to O by T which contains to $P$.


1. Trace the circumference $O$ ( radius $=3 \mathrm{~cm}$ ); $T$ is any inner point of the circumference.
2. Mark the point $P$ ( anyone outer to the circumference )
3. Trace the radius OT ; prolong it.
4. Trace the perpendicular bisector of the segment TP.
5. The perpendicular bisector cuts to radius OT in the centre $\mathrm{O}_{1}$
6. Trace the circumference $\mathrm{O}_{1}$; go over it.

## Tangency exercises 1 Sheet 4

a. Place $\mathrm{O}_{1}\left(\mathrm{r}_{1}=3 \mathrm{~cm}\right)$ and $\mathrm{O}_{2}\left(\mathrm{r}_{2}=4^{\prime} 5 \mathrm{~cm}\right) ;$ draw $\mathrm{O}_{3}\left(\mathrm{r}_{3}=2^{\prime} 5 \mathrm{~cm}\right)$

## Tangent to $\mathrm{O}_{1}$ And $\mathrm{O}_{2}$


b. Place two straight lines $h$ and $r$ which cut each other with a 60 degree angle; draw circumferences
$\mathrm{O}_{1}$ y $\mathrm{O}_{2}$ Tangent to both straight lines.


1. Trace an horizontal line (h)
2. Trace the inclined line $r$ ( forming a $60^{\circ}$ angle with $h$ )

3. Mark the centre $O_{1}$ : any point inner to bisector line.
4. Mark O , any point of the bisector line. Determine $\mathrm{T}_{2}$ y $\mathrm{T}_{2}$,
5. Determine the tangency points.
6. Trace $\mathrm{O}_{2}$ with centre $=\mathrm{O}_{2}$ y radius $=\mathrm{O}_{2} \mathrm{~T}$
